

# The Random Phase Approximation (RPA) and GW approximation for electrochemistry

The BEAST collaboration  
2<sup>nd</sup> Annual BEAST Workshop  
August 18, 2023



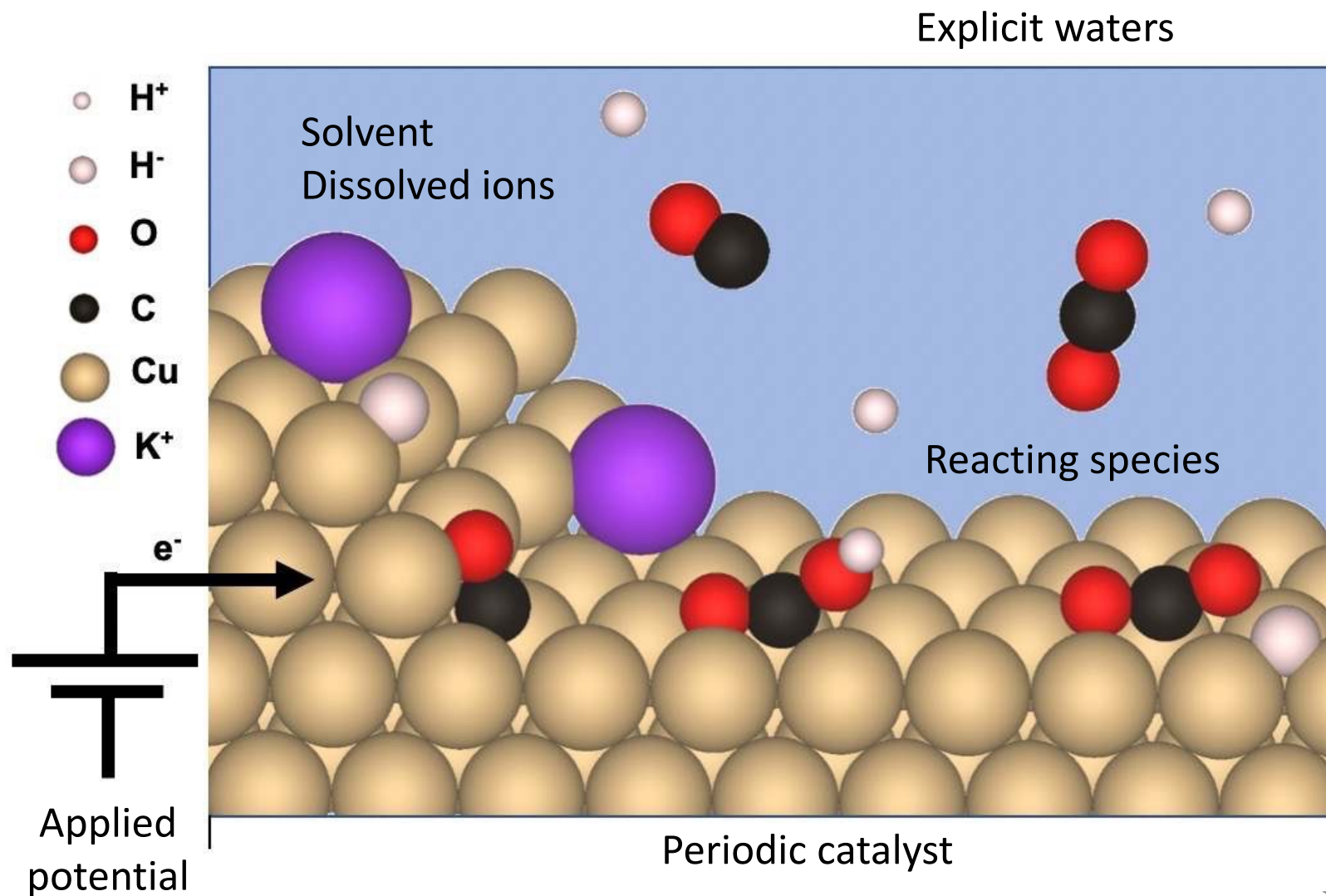
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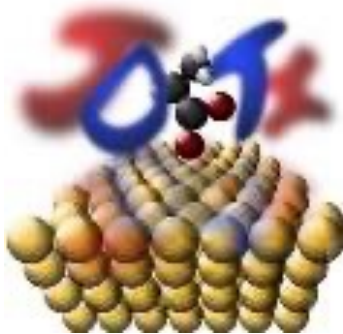
# Electrochemical systems are complex



# Density functional theory (Kohn-Sham)



- Predict ground state properties without empirical input
- Properties: structure, charge density, reaction energetics
- Thousands of practitioners worldwide (16k citations on Hohenberg, Kohn)
  - JDFTx, Quantum ESPRESSO, VASP, ABINIT, EXCITING, Fleur, Octopus, ELK



# Density functional theory (Kohn-Sham)

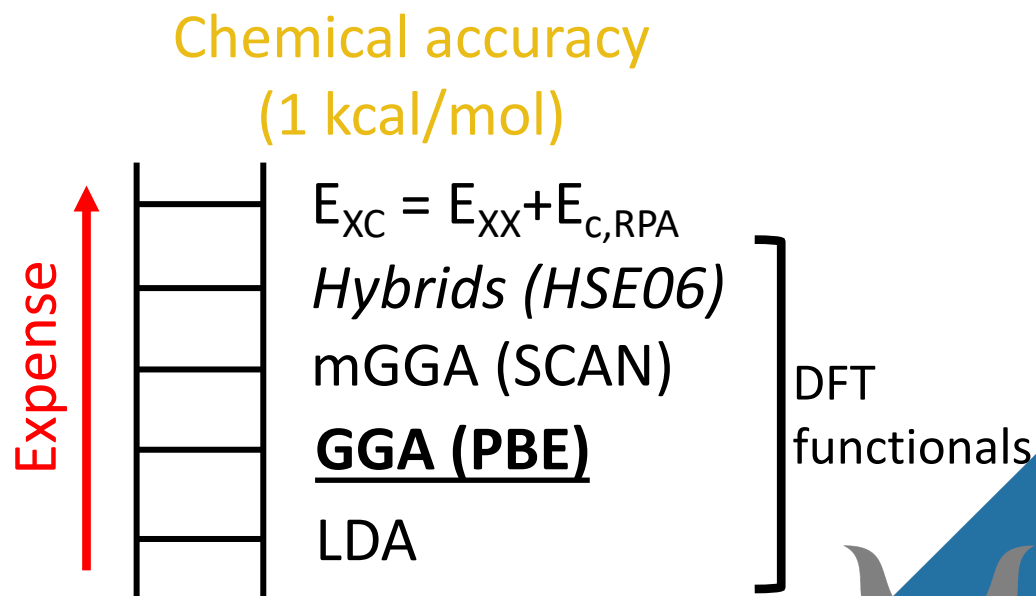


- Describing exchange-correlation term is key

$$\left(-\frac{1}{2}\nabla^2 + V_{ion} + V_{hartree}[n] + V_{xc}[n]\right)\psi_{nk} = \varepsilon\psi_{nk}$$

$$E_{DFT} = T_{KS} + E_{ion-el} + E_H + E_{XC}$$

- Calculate  $E_{XC}$  with varying degrees of accuracy/expense
  - 0 K, vacuum conditions

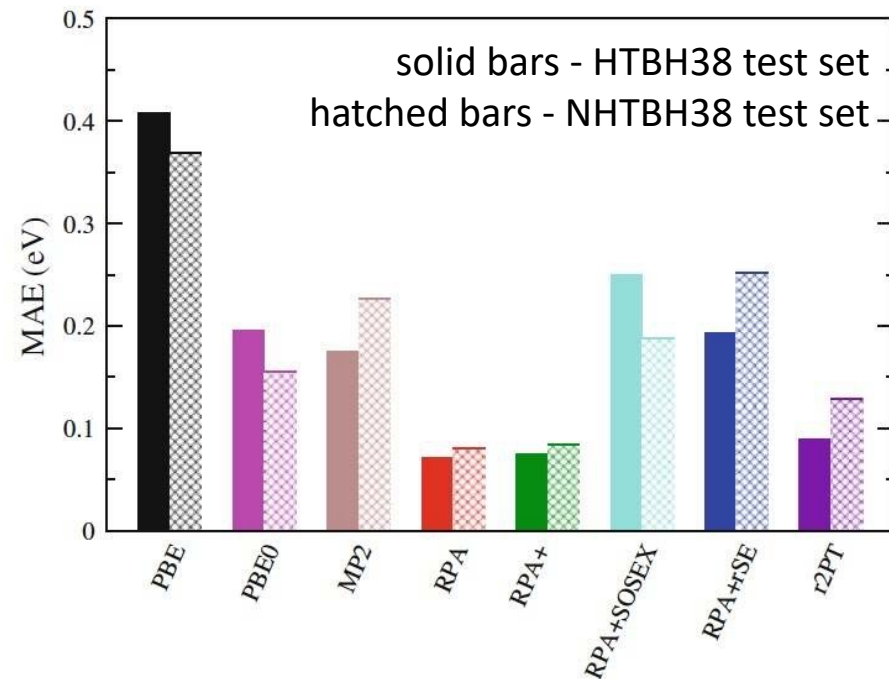
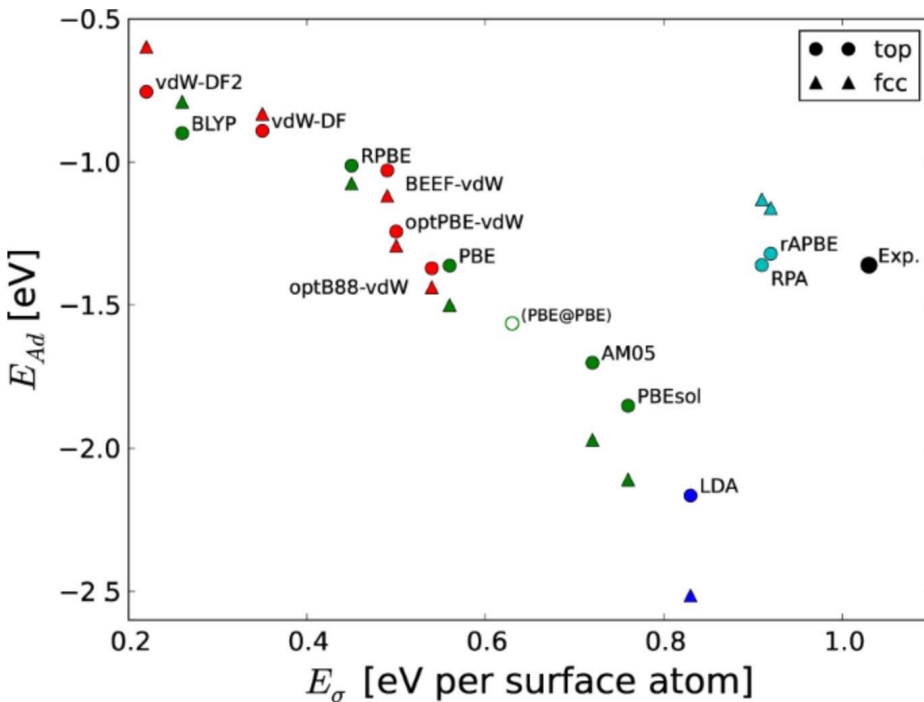


What functional gives accurate energies and electronic structure... generally?



# RPA can predict accurate properties relevant to catalysis

## CO adsorption to Pt(111)



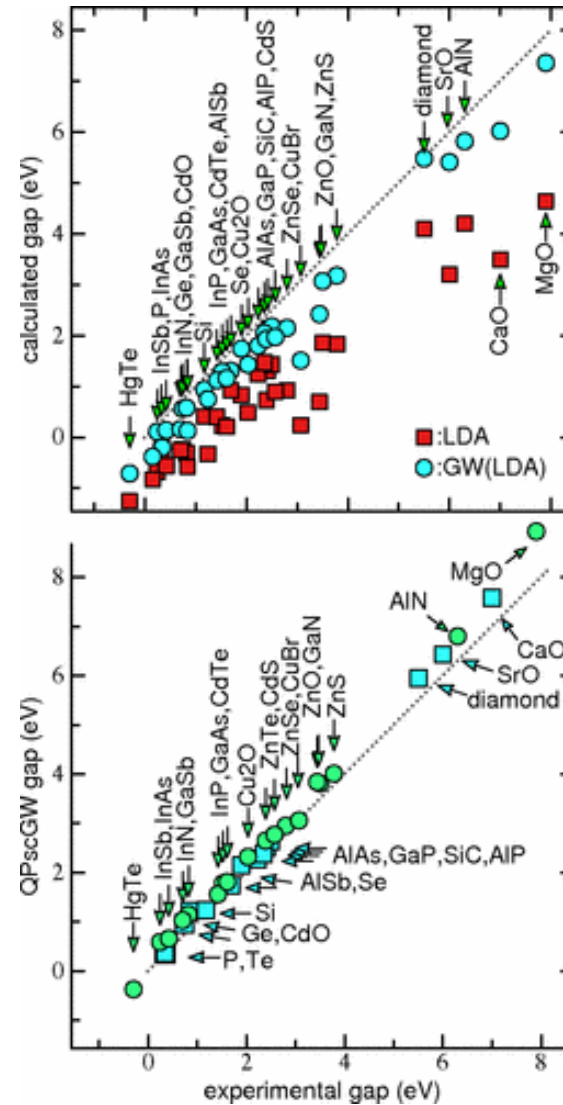
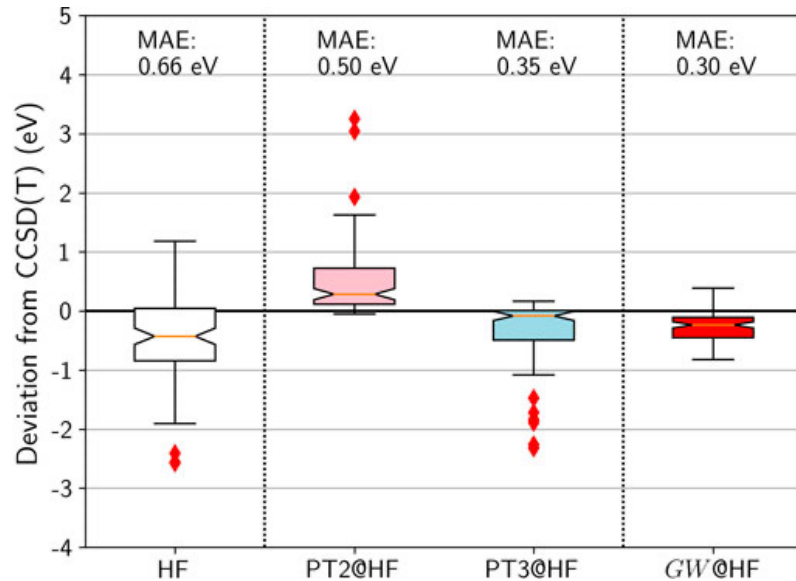
HTBH38: forward, inverse barrier heights of 19 hydrogen-transfer reactions, NHTBH38: 19 reactions involving heavy atom transfers, nucleophilic substitutions, association, unimolecular processes.

Olsen, et al., npj Computational Materials, 5 (2019)

Ren, et al., J. Mat. Sci., 47 (2012)



# GW can predict accurate IPs and band gaps



Bruneval, et al., Front. Chem. 9 (2021)  
 van Schilfgaarde, et al., PRL, 96, 226402 (2006)



# What is the GW approximation?

- Dyson equation: replace exchange-correlation potential with many-body self-energy

$$\left[ \frac{\nabla^2}{2} + V_{ion} + V_H + \Sigma(E_{nk}^{QP}) \right] \psi_{nk}^{QP} = E_{nk}^{QP} \psi_{nk}^{QP}$$

$$\Sigma = iGW$$

$$W_{GG'}(q; \omega) = \epsilon_{GG'}^{-1}(q; \omega) v(q + G')$$

$$\epsilon_{GG'}(q; \omega) = \delta_{GG'} - v(q + G) \chi_{GG'}^0(q; \omega)$$

- Polarizability calculated within random phase approximation



# Adiabatic Connection Fluctuation Dissipation Theorem (ACFDT)

- Non-interacting Hamiltonian constructed such that its ground state Slater determinant  $|\phi_0\rangle$  gives same density as true ground state wavefunction  $|\psi_0\rangle$

- Generalization of Kohn-Sham DFT: scale the coulomb interaction

$$v_c \rightarrow \lambda v_c \quad 0 \leq \lambda \leq 1$$

and obtain ground state wavefunction  $|\psi_0^\lambda\rangle$  gives same density as true ground state wavefunction  $|\psi_0\rangle$

$$|\psi_0^{\lambda=0}\rangle = |\phi_0\rangle \quad \text{and} \quad |\psi_0^{\lambda=1}\rangle = |\psi_0\rangle$$





# Key quantity: interacting polarizability $\chi^\lambda$

- Solve Dyson equation

$$\chi^\lambda(\omega) = \chi_{\text{KS}}(\omega) + \chi_{\text{KS}}(\omega) [\lambda v_c + f_{\text{xc}}^\lambda(\omega)] \chi^\lambda(\omega).$$

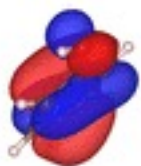
- The RPA:  $f_{\text{xc}}^\lambda = 0$
- Obtain polarizability
- Can calculate RPA correlation energy analytically

$$E_c^{\text{RPA}} = \int_0^\infty \frac{d\omega}{2\pi} \text{Tr} \left[ \ln \{ 1 - \chi^0(i\omega)v \} + \chi^0(i\omega)v \right]$$

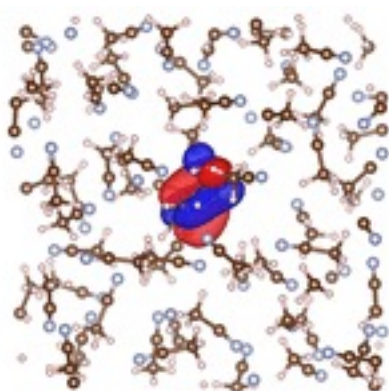


# Solvated beyond-DFT calculations are non-trivial

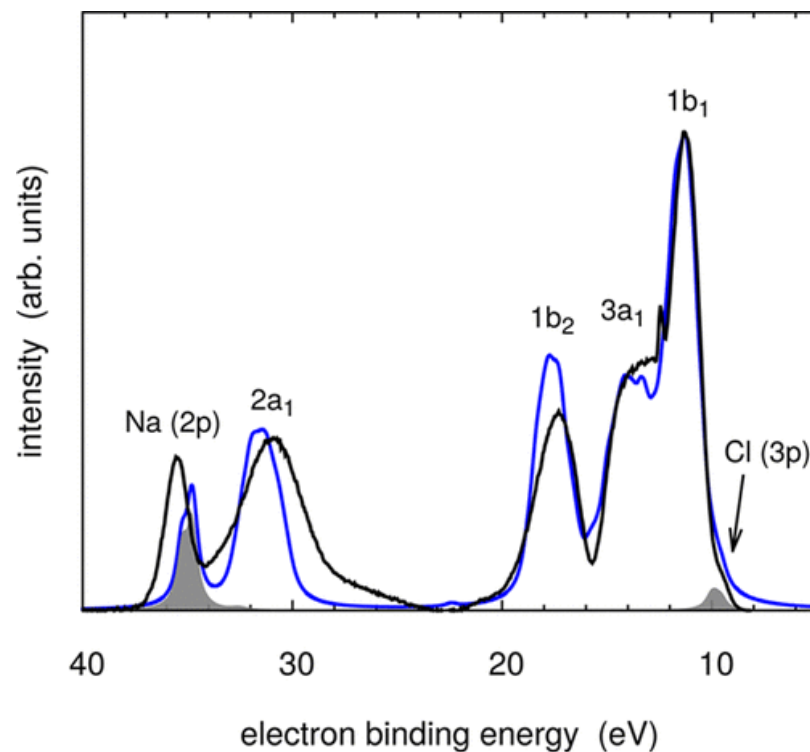
- Solvated GW calculations have previously used AIMD sampling of explicit waters or simplified implicit solvation models
  - 1 M NaCl = 1 Na + 1 Cl + 52 H<sub>2</sub>O

**a**

isolated phenol

**b**

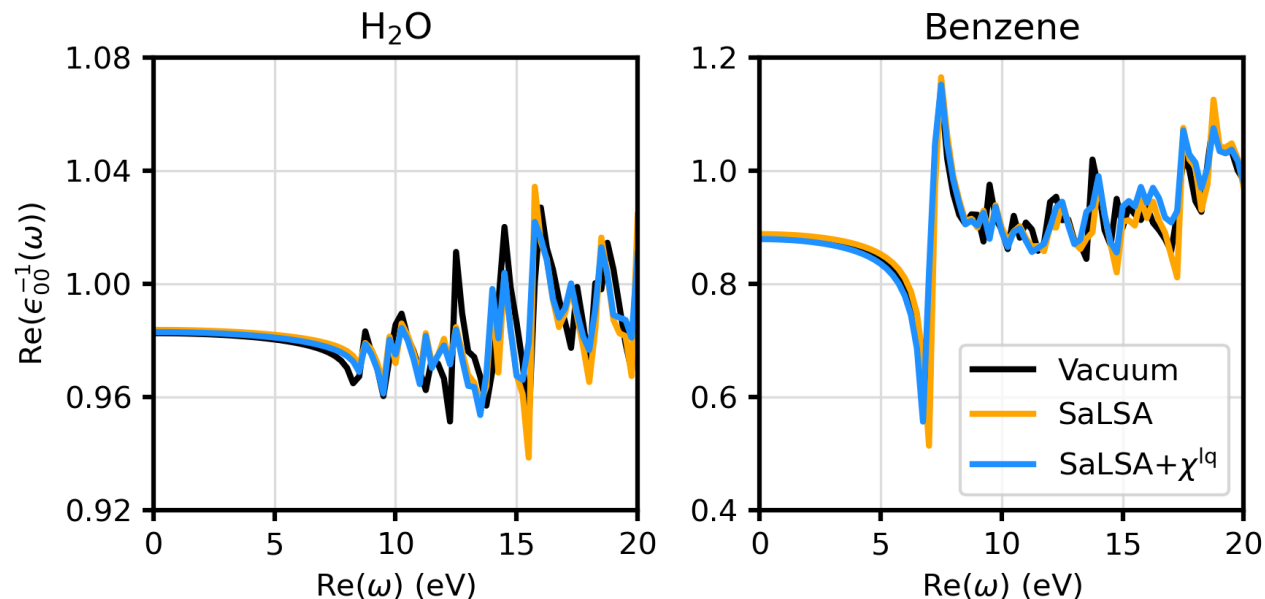
phenol in 64 ACN



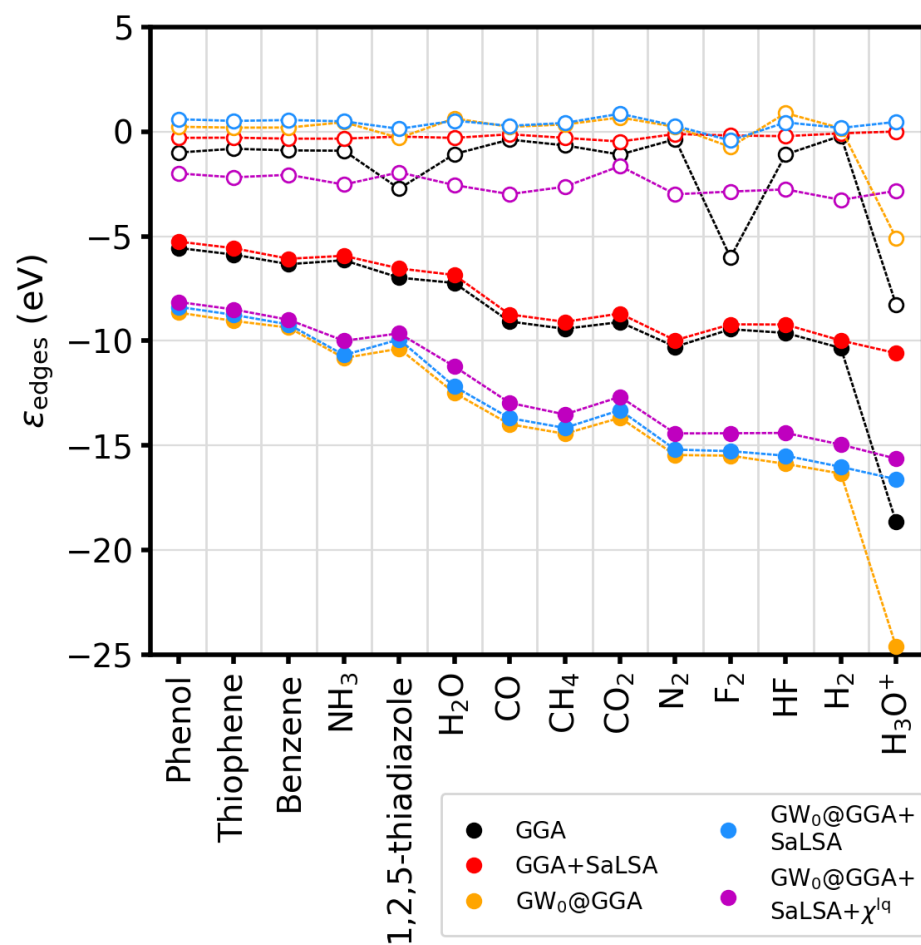
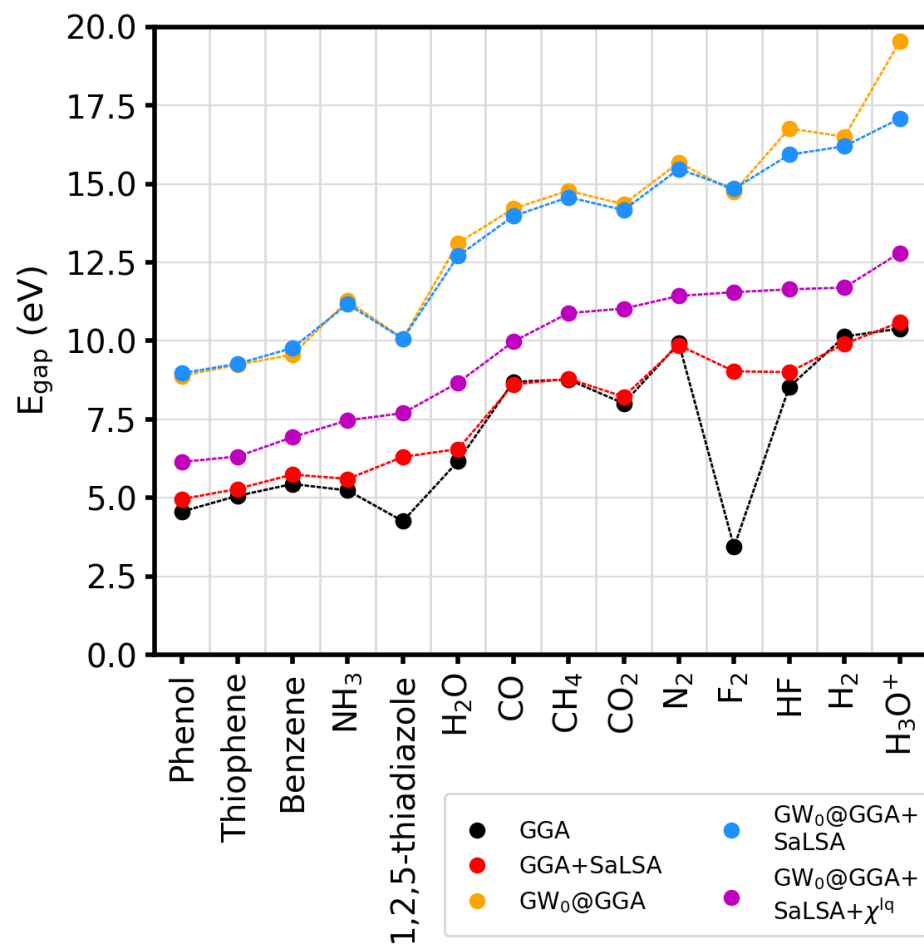
# Merging GW with advanced implicit solvation models

- We published a formalism merging GW with SaLSA model
  - Accepted paper should be available online soon
  - *Impact of solvation on the GW quasiparticle spectra of molecules*
- Use wavefunctions from solvated DFT calculation
- Combine fluid polarizability with electronic polarizability from SaLSA

$$\chi^{solv} = \chi^0 + \chi^{lq}$$



# Get lowering of HOMO-LUMO gap in molecules



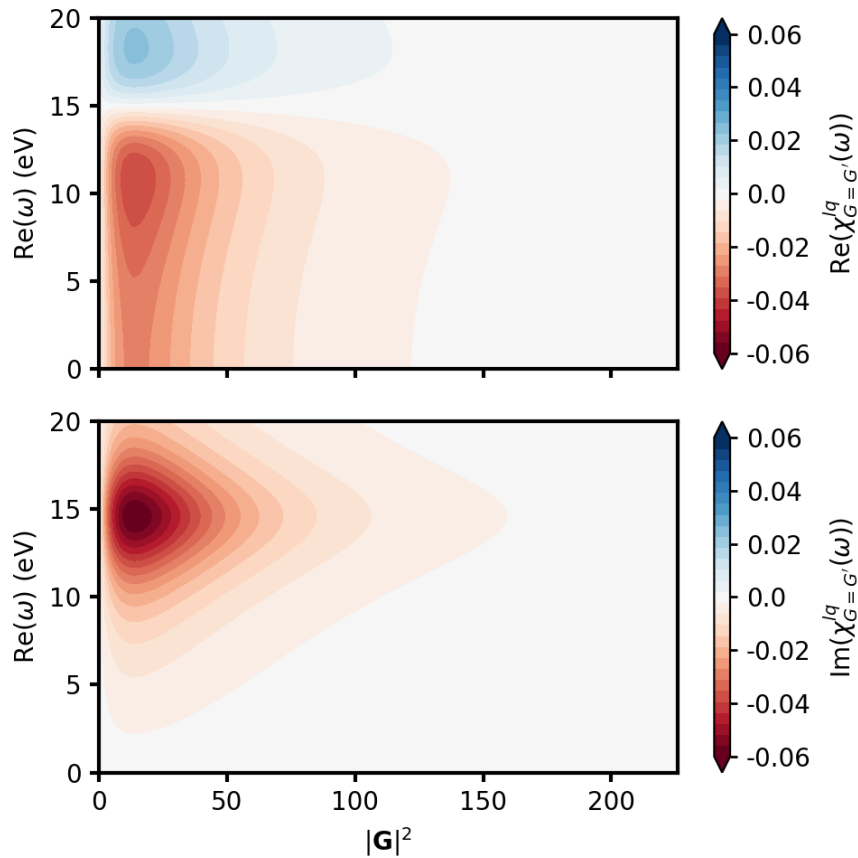
Get IP agreement with experiment where available

Molecule	IP	GW <sub>0</sub> @GGA+ SaLSA+ $\chi^{\text{LQ}}$ IP (eV)	Experimental IP (eV)
H <sub>2</sub> O	1 <sup>st</sup>	11.224	11.1 – 11.5 <sup>58–61</sup>
H <sub>2</sub> O	2 <sup>nd</sup>	13.468	13.5 – 13.8 <sup>59–61</sup>
H <sub>2</sub> O	3 <sup>rd</sup>	17.339	17.3 – 17.4 <sup>59,61</sup>
H <sub>3</sub> O <sup>+</sup>	2 <sup>nd</sup>	20.619	20 – 21 <sup>62</sup>
Phenol	1 <sup>st</sup>	8.141	7.8 – 8.3 <sup>63,64</sup>
Phenol	2 <sup>nd</sup>	8.924	8.6 <sup>63</sup>

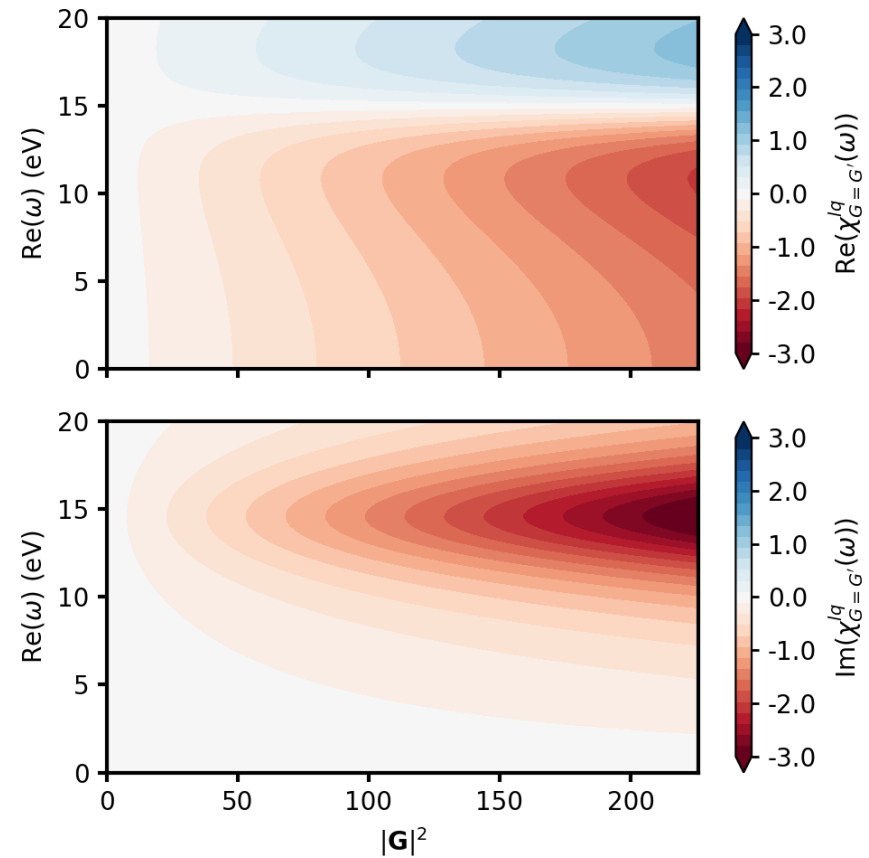


# Have to use SaLSA currently to avoid divergence

## SaLSA



## GLSSA13



# Current work: can we extend this to RPA?

- Features

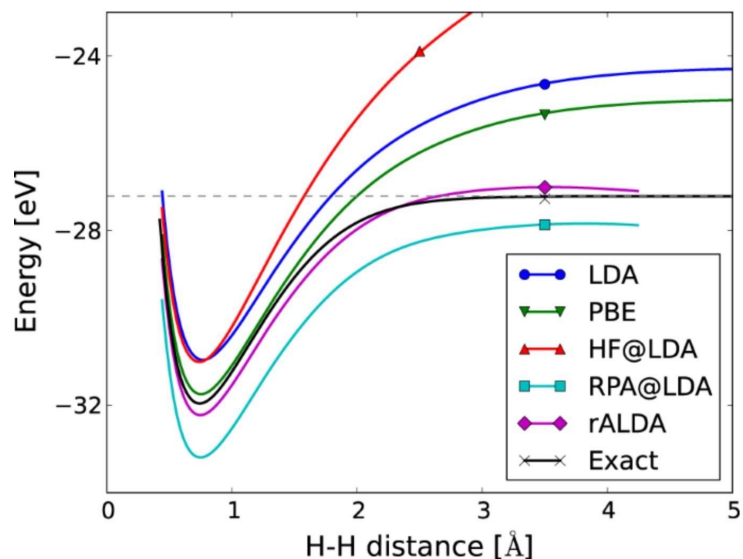
- RPA gives correlation energy, compute EXX using input orbitals
- Exactly cancels self-interaction from Hartree term (some self-interaction in correlation)
- $O(N^4)$  complexity: between DFT and high-fidelity MP2, CCSD, CCSD(T)
- Parameter-free dispersion forces: key for surface chemistry, binding of 2D materials

- Shortcomings

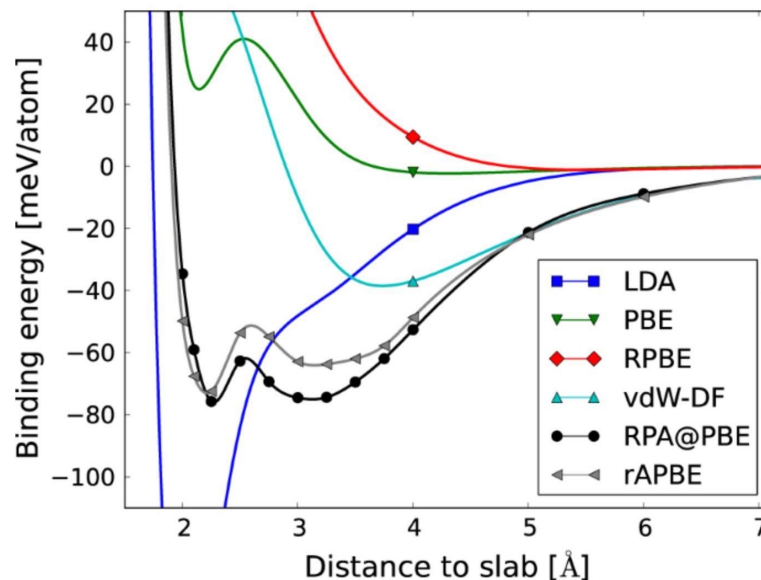
- So-so short-range correlation: inaccurate cohesive energies, atomization energies
- Slow convergence with kinetic energy cutoff (wavefunction cusp condition)



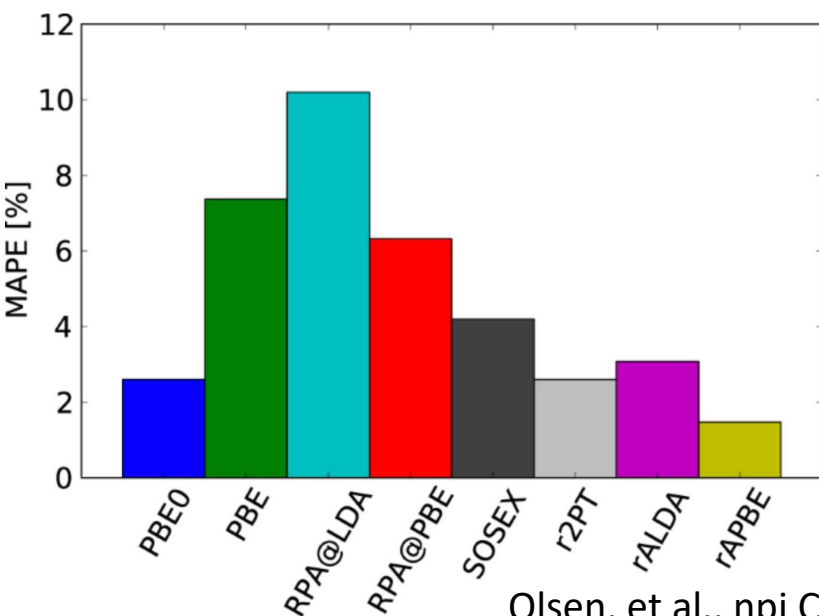
## H<sub>2</sub> dissociation: RPA good



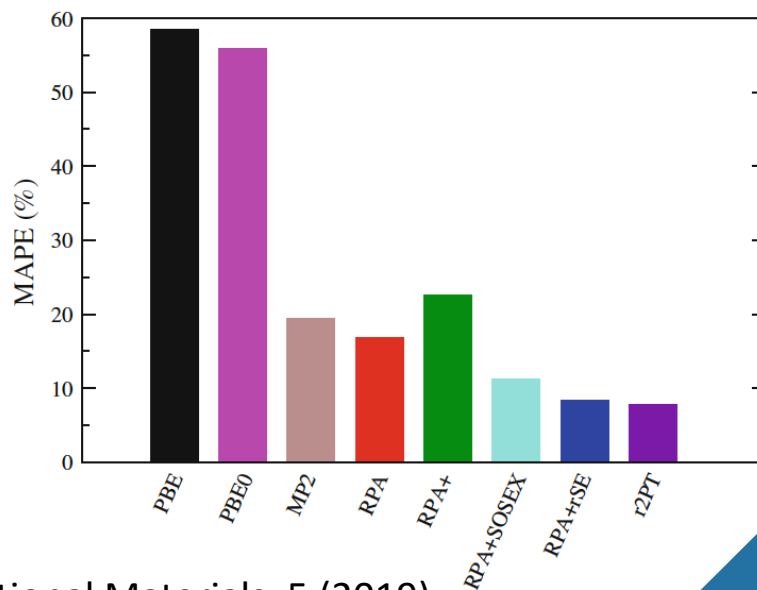
## Graphene\*+Ni(111): RPA good



## Atomization energies: RPA ok



## vdW/H-bonding: RPA very good





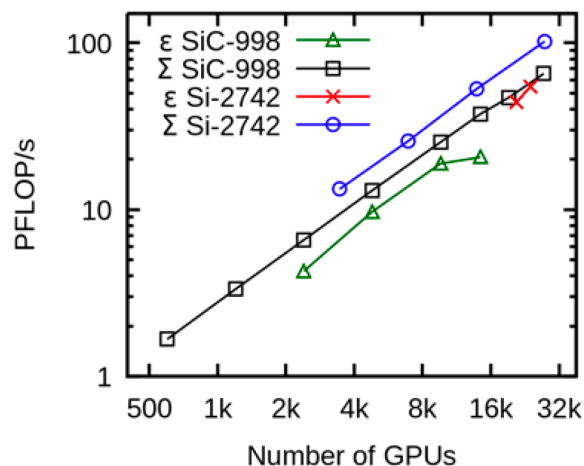


# BerkeleyGW On the Path to Exascale

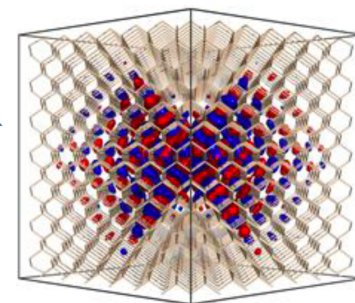
Foreseen exascale HPC systems will be GPU accelerated architectures

Optimized version of BerkeleyGW on GPU accelerated systems:

- Scale up to the full Summit machine at OLCF: **>27k GPUs**
- Reach nearly 53% of the peak performance at **106 PFLOP/s**
- Time to solution of **~10 mins for 11k electrons system**



M. Del Ben, C. Yang, Z. Li, F. H. da Jornada, S. G. Louie and J. Deslippe, "Accelerating Large-Scale Excited-State GW Calculations on Leadership Class HPC Systems" in Proceedings of the International Conference for High Performance Computing, Networking, Storage and Analysis, ser. SC '20 No.4 pp.1 (2020), ACM Gordon-Bell Finalist



Divacancy defect in semiconductor (such as Si and SiC) are proxy for solid state Qubits. For silicon shown is the 2742-atoms Si supercell, 10,968 electrons.